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Structures and Electronic Properties of TiV (N=1-16) Clusters: First-Principles Calculations

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Structures and Electronic Properties of Ti_nV ($n=1-16$) Clusters: First-Principles Calculations

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Abstract

Structures and electronic properties of Ti_nV ($n = 1 - 16$) clusters have been investigated using density functional theory (DFT) with the generalized gradient approximation (GGA). The calculations have shown that the Ti_nV clusters favor compact spherical structures having similar conformations to the pure Ti_n clusters. The results show that the vanadium atom remains on the surface when $n \leq 8$ and $n = 16$, while for $n = 9 - 15$, it occupies the endohedral position. The Ti_6V , Ti_{12}V , and Ti_{14}V clusters are found to be more stable than their neighbors, consistent with pure Ti_n clusters that have the same size. Additionally Ti_4V has been found to be also magic, consistent with recent reports of B and Al-doped Ti clusters. Small Ti_nV ($n \leq 4$) clusters exhibit a transition from metallic-like to semi-metallic electronic structure, while for $n = 5$ onwards, no significant changes are observed compared to pure Ti_n clusters.

Keywords

TiV clusters, Titanium, Density functional theory, DFT

Introduction

Subnanometer clusters are considered a new phase of matter, being the bridge between atoms and the bulk. They form part of an extensive research due to various potential applications.^{1,2} It has been found that atomic clusters for a wide type of elements are suitable to undertake catalytic reactions including gold, which is practically inert in the bulk, and the capability of gold to be reactive is one of its most attractive properties.^{3,4} There is considerable interest in the structures and properties of subnanometer clusters for example for their use as finely divided metal catalysts, particularly for bimetallic clusters, which offer the opportunity of tuning their activity and selectivity. To date, much work has concentrated on small clusters of late transition metals e.g. noble and platinum metals, while little has been

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3 done for the early transition metals. Among transition metal (TM) clusters, the reactivity
4 of titanium clusters is not fully understood, due to the complexity of the almost empty d
5 band which provide unique bonding properties.⁵ Recently, a number of studies of titanium
6 clusters were focused in studying the physical and electronic properties. Early experiments
7 on Ti_2 clusters by⁶⁻⁹ revealed that the binding energy varies from 2.1 to 1.05 eV, which
8 was considered as the lowest limit by Haslett et al.⁷ In 1980, C. Cossé et al. determined
9 the Raman spectrum of the isolated Ti_2 dimer.¹⁰ Sakurai et al.¹¹ determined that $N = 7,$
10 13, 15, 19 and 25 are magic numbers of titanium clusters. Wu et al.¹² performed anion
11 photoelectron spectroscopy experiment for Ti_n clusters with $n = 2 - 65$. Theoretically, Wei
12 et al.¹³ studied Ti clusters up to $n = 10$ using density functional theory (DFT) and came to
13 the conclusion that the electronic structures of the titanium clusters develop some bulk-like
14 features at rather small size. Zhao et al.¹⁴ studied the structures and electronic properties
15 of Ti_n clusters ($n = 2 - 14, 19, 55$) by the plane wave ultrasoft pseudopotential method
16 suggesting that Ti clusters favor a pentagonal growth pattern. Villanueva et al.¹⁵ studied
17 Ti_n clusters from $n = 2 - 15$ using DFT with the Lee-Yang-Parr (LYP) functional and found
18 that Ti_7 and Ti_{13} clusters show higher stability than other clusters, which has been confirmed
19 with experiments. Ascencio et al.,¹⁵ identified three magic number clusters $\text{Ti}_7,$ Ti_{13} and
20 $\text{Ti}_{15},$ corresponding to closed-packed structures. In spite of the number of works based on
21 Ti clusters, a few studies on doped Ti clusters were carried out in both experiment and
22 theory. This may be due to the existence of d electrons, since the size-dependent variations
23 cannot be explained by the shell models of s valence electrons.¹⁶ Recent studies showed that
24 the chemical and electronic properties of titanium clusters could be tuned by doping. In
25 particular, doped titanium clusters with formula Ti_{12}M have shown higher stability when
26 the dopant M turns out to be placed at the center of the cage, which can be understood from
27 the pseudo-spherical icosahedral structure, which has been observed with a high stability for
28 other metallic clusters. Xiang et al.¹⁷ studied Al-doped Ti_n clusters using density functional
29 theory and found that the Al remains on the surface of the clusters for $n < 9,$ while it occupies
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3 the center of the cage for $n = 9$ onwards. J. Du et al.¹⁸ studied B-doped Ti_n clusters and
4 found that the isomers with a B atom located on the surface are energetically favored for
5 most of the studied clusters except $Ti_{12}B$. Furthermore, J. Du et al. demonstrated that
6 the electron transfers from Ti atoms to the impurity contributes for the stability of Small
7 M-doped Ti_{1-4} clusters ($M = V, Fe, Ni$),¹⁹ however, as far as we know, the structures and
8 electronic properties of larger Ti_nV clusters (that have $n > 4$) are not investigated until
9 now. In this work, we studied the growth behaviour of Ti_nV ($n = 1 - 16$) clusters and found
10 that the $Ti_{n-1}V$ clusters hold similar structural conformations than the bare Ti_n clusters.
11 It turns out that the V impurity remains on the surface when $n \leq 8$ and $n = 16$, while for
12 $n = 9 - 15$, it occupies the cage center. The analysis of the binding energy indicates that the
13 Ti-V bond strength increase for clusters with $n = 11 - 13$ atoms, especially for $Ti_{12}V$, which
14 adopts the icosahedral geometry. The electronic structures of small Ti_nV ($n \leq 4$) clusters
15 exhibit a transition from metallic-like to semi-metallic electronic structure, while for $n = 5$
16 onwards, no significant changes are observed compared to pure Ti_n clusters.
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34 Computational Details

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37 In metal clusters all their physical and chemical properties depend on its structure, and their
38 determination is one of the most fundamental and important tasks. The determination of
39 the most stable structure requires finding the global minimum of the potential energy surface
40 (PES), which gives the energy of a system as a function of its atomic coordinates.²⁰ For this
41 task, almost all algorithms require an enormous number of evaluation of PES, thus a sys-
42 tematic search for the global minimum is necessary. Various levels of theory have been used
43 with the aim of predicting the structure of TM clusters. Empirical potentials are not always
44 reliable for structure prediction because they typically neglect the directional nature of $d-d$
45 interactions and quantum effects such as those arising from spin magnetism, orbital symme-
46 try, and electronic shell closings.²¹ It is because of this that we use the *ab initio* method to
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3 describe the partially filled d shells and strong electron correlation. For the evaluation of PES
4 a set of initial structures are obtained using graph theory with the methodology described
5 in our previous work,²² which allows us to explore the configuration space for small clusters
6 ($n \leq 7$). We systematically generate the Ti_nV alloy structures for a given cluster size by re-
7 placing the V impurity in all Ti positions of the initial structures. For each size, the center of
8 mass and number of Ti-V, and homogeneous Ti-Ti bonds is compared. This procedure allow
9 us to reduce the number of isomorphic structures. All the resulting structures are optimized
10 by *ab initio* calculations. From $n = 8$ onwards, the structures of Ti_nV clusters are con-
11 structed based on those of smaller doped clusters by adding a single atom on all inequivalent
12 binding sites on the surface of the equilibrium structures of Ti_{n-1}V clusters. This procedure
13 however, generates a large number of structures, increasing the computational complexity,
14 because of this, we only decorate stable clusters whose relative energy is less than $\Delta E = 1$
15 eV from the ground state. The principle of this procedure is that the clusters follow a growth
16 pattern from the preceding ones. The calculations in this work are based on the framework
17 of spin-polarized density functional theory (DFT)^{23,24} implemented in the code Vienna *ab*
18 *initio* simulation package (VASP),^{25,26} which solves the Kohn-Sham equations under peri-
19 odic conditions with a plane wave basis set. The interactions between the ions and valence
20 electrons are described by the projector augmented-wave (PAW) method.²⁷ The exchange
21 correlation (XC) functional is treated using the PBE approximation.²⁸ The wave functions
22 are expanded in plane-wave basis sets with a cutoff energy of 400 eV. The atomic positions
23 are relaxed self-consistently by the conjugate gradient method algorithm until the forces are
24 smaller than 0.01 eV/Å for all atoms. We used a supercell with a distance of 10 Å of vacuum
25 between periodic images, which is large enough to avoid their interaction. Due to the size of
26 the supercell, only the Γ point is taken into account to represent the Brillouin zone. For the
27 finding of the global minimum PES of Ti_nV clusters, for each structure multiple spin states
28 are considered. For each cluster size, the local minima of the potential energy surface on
29 the lowest energy configuration is proven by the harmonic vibrational frequencies. To check
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the accuracy of our calculation, the binding energy and bond length of Ti_2 and TiV dimers are compared with theoretical and experimental values as shown in Table 1. Additionally, for the calculation of the anionic state, a background charge was applied to maintain charge neutrality. The dipole and quadrupole moment corrections were taken into account²⁹ to properly screen out long range Coulomb interactions.

Table 1: Calculated equilibrium bond length and binding energy for Ti_2 , and TiV dimers in the ground state configuration.

Dimer	Method	Functional	Bond length (Å)	Binding energy (eV/at.)
Ti_2	PAW ^a	PW91	1.92	1.61
	<i>all-electron</i> ^b	PW91	1.958	2.57
	This work	PBE	1.897	1.875
	US PP ^c	GGA (PW)	1.92	2.34
	Expt. 1 ^d		1.943	-
	Expt. 2 ^e		-	1.54 ± 0.19
TiV	This work	PBE	1.788	1.875
	LCAO ^f	BPBE	1.838	2.27

^a Ref.³⁰

^b Ref.¹⁸

^c Ref.¹⁴

^d Ref.³¹

^e Ref.³²

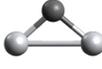
^f Ref.¹⁹

Results and discussion

The equilibrium structures of the pure Ti_n clusters that have $n = 2 - 17$ are optimized on the basis of previous calculation results. Anderson³³ concluded that titanium clusters have tightly packed structures by using the molecular orbital method, which is in good agreement with our result. Our calculation shows that the most stable structure of Ti_3 is an equilateral triangle with D_{3h} symmetry. The stable structures of Ti_{4-6} are an axially distorted tetrahedron with C_{3v} symmetry, a distorted trigonal bipyramid (TBP) structure with C_{2v} symmetry, and a C_{2v} octahedron, respectively. In accordance to Wei et al. these clusters have not regular symmetries like a regular tetrahedron (T_d) trigonal bipyramid (D_{3h}) and octahedron (O_h). In contrast, for Ti_6 , J. Du et al. found a C_{2v} structure with $4 \mu_B$

as the ground state. Ti_7 is a pentagonal bipyramid (PBP) structure with a singlet state. For Ti_8 , a bicapped octahedron with D_{2d} symmetry is the most stable structure. For Ti_9 to Ti_{12} clusters, the ground state is formed by a partial icosahedron structure. The ground state of Ti_{13} is formed by a Jahn-Teller distorted icosahedral structure with $6 \mu_B$, while the most stable structure of Ti_{15} is a bicapped hexagonal antiprism with $4 \mu_B$ of total magnetic moment. Ti_{14} is a capped icosahedron. For $n = 16$ and 17, we found a closed-packed structure for the Ti_n clusters, which is expected due to the delocalization of $3d$ electrons. In order to determine the effect of the V impurity, we used the results of the bare Ti_n clusters as reference systems. As far as we know, the structures of V-doped Ti_n (with $n > 4$) clusters are not investigated so far, it is because of this that we have performed an extensive search to find the minimum energy structure described in the previous section.

Table 2: Ground-state structures and low-lying isomers of Ti_n and Ti_{n-1}V ($n = 3 - 6$) clusters. For each cluster the total magnetic moment (in μ_B), and the binding energy (eV) is given. The gray and dark spheres represent Ti and V atom, respectively.

			
3a ₀ , 6 μ_B 2.342 eV	3a, 1 μ_B 2.307 eV	3b, 5 μ_B 2.160 eV	4a ₀ , 4 μ_B 2.808 eV
			
4a, 5 μ_B 2.659 eV	4b, 1 μ_B 2.649 eV	5a ₀ , 2 μ_B 3.129 eV	5a, 1 μ_B 3.087 eV
			
5b, 1 μ_B 3.065 eV	6a ₀ , 2 μ_B 3.275 eV	6a, 1 μ_B 3.292 eV	6b, 1 μ_B 3.292 eV

The lowest energy structures and some metastable low-energy isomers (from Ti_2V to Ti_5V) are presented in Table 2, including their Ti_n cluster counterpart for comparison. Each structure is labeled with a number and a letter corresponding to the total number of atoms, and the alphabetic order is attached to the isomers in descending order of cluster stability.

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4 The structures of pure Ti_n are also included in Table 2 as well as the binding energy per
5 atom (E_b), and total magnetic moment (μ). The ground state structure of the TiV dimer
6 is a triplet state with a binding energy of 1.87 eV/atom and Ti-V bond length of 1.78 Å
7 shorter than that of the Ti_2 dimer, with 1.89 Å. Using the BPBE functional, J.G. Du et al.¹⁹
8 obtained a bond distance of 1.838 Å for the TiV dimer, which is in close agreement with our
9 result. They found a dissociation energy of 2.27 eV/atom, which is slightly larger than the
10 calculated in the present work. The Bader charge analysis indicates that a charge transfer
11 occurs from the Ti atoms to the V impurity, consistent with Ref. 19. This behaviour may
12 derive from the larger electronegativity of V (1.63), with respect to Ti atom (1.54). The
13 ground state structure of Ti_2V is an open triangle with 98.4° for the \angle Ti-V-Ti angle and
14 with Ti-V distances of about 1.83 Å. The magnetic moment is $1 \mu_B$, which is significantly
15 lower than Ti_3 with $6 \mu_B$. For the Ti_3V cluster the most stable structure is a tetrahedron
16 with $5 \mu_B$, while a planar rhombus with $1 \mu_B$ is only 0.04 eV higher in energy. Ti_4V and
17 Ti_5V clusters are formed by a TBP and an irregular octahedron (O_H) structure, respectively.
18 Notice that from Ti_2V to Ti_5V clusters, the doped clusters have the same conformation than
19 the bare Ti clusters where the V impurity occupies the top site. The ground-state geometries
20 and isomers of clusters (from Ti_6V to $Ti_{11}V$) are shown in Table 3. In the case of Ti_6V , the
21 most stable structure (7a) is a PBP, in which the V atom occupies the most coordinated
22 position, which is 0.09 eV more stable than the 7b isomer, in which the V impurity is located
23 in the vertex site. A bicapped octahedron is obtained for Ti_7V as the lowest energy structure,
24 where the V atom occupies the surface site. For Ti_8V , a bicapped PBP is the most stable
25 structure. The most stable structures of $Ti_{9-11}V$ clusters have an icosahedral growth, where
26 the V impurity is trapped on the center of the cluster conserving the shape of the host
27 cluster, except for $Ti_{10}V$ in which the structure is slightly distorted.
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52 The ground-state geometries and isomers of clusters (from $Ti_{12}V$ to $Ti_{16}V$) are shown in
53 Table 4. The most stable structure of $Ti_{12}V$ can be considered as a distorted icosahedral
54 structure, but not a regular icosahedron (I_h) in which the impurity is located in the center of
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Table 3: Ground-state structures and low-lying isomers of Ti_n and $Ti_{n-1}V$ ($n = 7 - 12$) clusters. For each cluster the total magnetic moment (in μ_B), and the binding energy (eV) is given. The gray and dark spheres represent Ti and V atom, respectively.

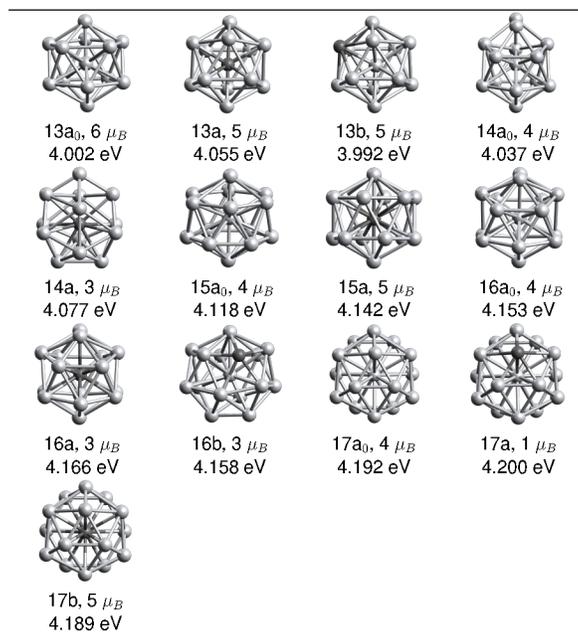
			
7a ₀ , 0 μ_B 3.474 eV	7a, 1 μ_B 3.487 eV	7b, 1 μ_B 3.474 eV	8a ₀ , 4 μ_B 3.487 eV
			
8a, 1 μ_B 3.563 eV	9a ₀ , 2 μ_B 3.660 eV	9a, 1 μ_B 3.641 eV	9b, 1 μ_B 3.629 eV
			
10a ₀ , 4 μ_B 3.718 eV	10a, 1 μ_B 3.699 eV	11a ₀ , 4 μ_B 3.794 eV	11b ₀ , 10 μ_B 3.649 eV
			
11a, 1 μ_B 3.809 eV	11b, 1 μ_B 3.795 eV	12a ₀ , 2 μ_B 3.886 eV	12a, 1 μ_B 3.922 eV

the cage. This feature has been observed for $Ti_{12}M$ clusters when doped with $M=B$ and Al , while for the other sized clusters, the impurity usually adopts the surface site. The $Ti_{12}V$ isomer in which the V atom occupies the surface site is about 0.83 eV higher in energy. In $Ti_{13-15}V$ clusters the V impurity is also trapped in the center of the cluster. Nevertheless, for $Ti_{16}V$, which is the largest cluster considered in this work, the V impurity occupies the surface site. It is interesting to note that the structures of the Ti_nV clusters can be obtained by adding an impurity atom on the most stable Ti_n clusters.

Electronic structure

The stability of Ti_n and Ti_nV clusters is investigated by calculating the binding energy per atom (E_b), second order energy differences (Δ_2E), and dissociation energy (E_d), defined as

Table 4: Ground-state structures and low-lying isomers of Ti_n and $Ti_{n-1}V$ ($n = 13 - 17$) clusters. For each cluster the total magnetic moment (in μ_B), and the binding energy (eV) is given. The gray and dark spheres represent Ti and V atom, respectively.



$$E_b[Ti_n] = [nE_T(Ti) - E_T(Ti_n)]/n, \quad (n = 2, 3, \dots, 17) \quad (1)$$

$$\Delta_2 E[Ti_n] = E_T[Ti_{n+1}] + E_T[Ti_{n-1}] - 2E_T[Ti_n], \quad (2)$$

$$E_d[Ti_n] = E_T[Ti_{n-1}] + E_T[Ti] - E_T[Ti_n], \quad (3)$$

for the pure Ti_n clusters, and

$$E_b[Ti_nV] = (nE_T[Ti] + E_T[V] - E_T[Ti_nV])/(n + 1), \quad (n = 1, 2, \dots, 16) \quad (4)$$

$$\Delta_2 E[Ti_nV] = E_T[Ti_{n+1}V] + E_T[Ti_{n-1}V] - 2E_T[Ti_nV], \quad (5)$$

$$E_d[Ti_nV] = E_T[Ti_{n-1}V] + E_T[Ti] - E_T[Ti_nV], \quad (6)$$

for the V-doped Ti_n clusters, where $E_T[Ti]$, $E_T[V]$, and $E_T[Ti_nV]$ are the total energies of the bare Ti atom, the V atom, the Ti_nV doped cluster, while n denotes the number of Ti atoms in the cluster, respectively. The Figure 1 shows the binding energy of pure Ti_n and $Ti_{n-1}V$ clusters for $n = 2 - 17$. For the bare Ti_n clusters, E_b gradually increases with the cluster size n rapidly up to $n \leq 7$ and then the size dependence become smooth at $n > 7$. When Ti clusters are doped with V, the binding energy is similar for $Ti_{1-10}V$ clusters, except for Ti_3V and Ti_6V clusters, where it is lower than for pure Ti_n clusters. Interestingly, for $Ti_{12}V$ and its first neighbors, the binding energy is slightly larger, while for $n = 15$ onwards the Ti clusters become more stable. The increased stability of the $Ti_{12}V$ cluster can be understood by the icosahedral structure of $Ti_{12}V$. The high stability of the regular icosahedral structure usually occur for transition metal clusters. In a recent paper by us, we found that the icosahedral structure has a special reactivity when compared with less coordinated structures.²²

The second order energy difference Δ_2E and dissociation energy E_d help us to determine the relative stability of Ti_nV clusters compared with their neighbors. For Δ_2E and E_d (see Figures 2a and 2b), an odd-even pattern is shown with the maximum values at $Ti_{12}V$ followed by $Ti_{14}V$, Ti_6V , and possibly Ti_4V clusters. Those sizes correspond to the magic numbers of Ti_6 , Ti_{13} and Ti_{15} clusters, in excellent agreement with previous theoretical and experimental results. Interestingly, J. Xiang et al. found that Ti_4Al is also magic, which supports our finding for the Ti_4V cluster. As in Eq. 6, we calculated the V dissociation energy $E_d[V]$ as shown in Figure 2c, and found similar energy variation than for the Ti dissociation energy.

It is very interesting to mention that anionic Ti_n^- and neutral Ti_nV clusters are isoelectronic but differ in one component atom. To compare the differences between them, we calculated the anionic Ti_n^- clusters based on the structure isomers of the neutral Ti_n and Ti_nV clusters considering five spin multiplicities. Additionally, we calculated the electron

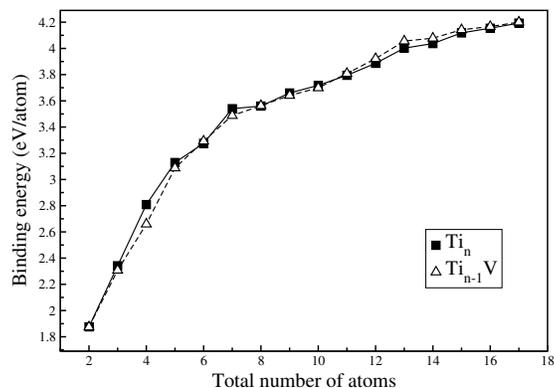


Figure 1: Comparison of the binding energies of Ti_n and $Ti_{n-1}V$ clusters. Note that we are comparing clusters with the same size, (e.g. for $n = 6$, Ti_6 and Ti_5V lie at the same value).

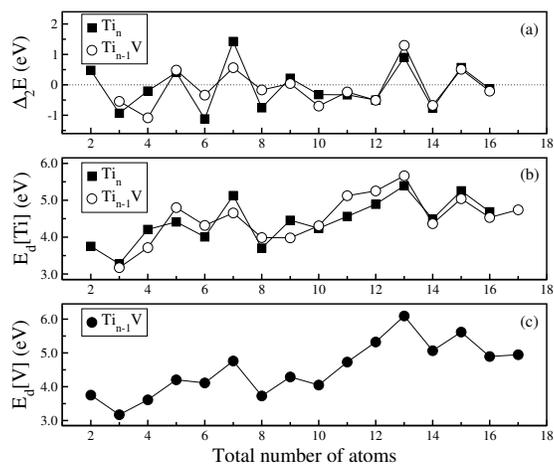


Figure 2: (a) Comparison of the second difference of the most stable Ti clusters as a function of n , (b) Ti dissociation energy $E_d[Ti]$ for Ti_n (Eq. 3) and $Ti_{n-1}V$ (Eq. 6) and (c) V dissociation energy $E_d[V]$ for $Ti_{n-1}V$ as a function of the cluster size n .

affinity (EA), which is an important quantity to characterize metal clusters, defined as

$$EA_n = E_T(Ti_n) - E_T(Ti_n^-), \quad (7)$$

where $E_T(Ti_n)$ and $E_T(Ti_n^-)$ are the total energies of the neutral Ti_n and anionic Ti_n^- clusters. In Figure 3a we show EA_n of Ti_n^- clusters as a function of size. We found smaller values than the experimental reported ones, but closer than a recent DFT calculation by Kummar et al.⁵ EA_n increases gradually with the size with a minimum at $n = 7$, in agreement with the experimental data.³⁴ We found that Ti_n^- clusters favor the structures of the neutral Ti_n clusters rather than that of the V doped Ti_n ones. In Figure 3 we also show the calculated second order energy differences of Ti_n^- clusters and found that their stability is more sensitive to the size than that of the neutral Ti_nV ones (as shown in Figure 2a).

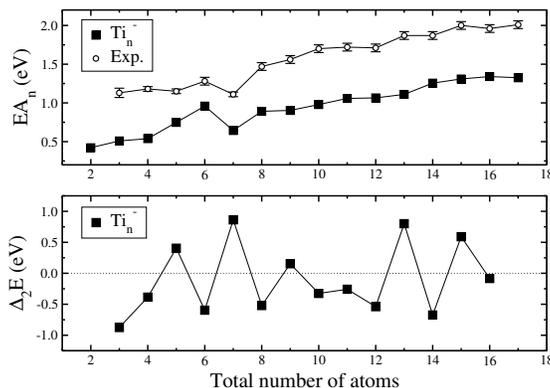


Figure 3: The EA_n (top) and Δ_2E (bottom) of the most stable anionic Ti_n^- clusters is presented.

In order to have some insight into bonding nature, we show the Ti-V and Ti-Ti average bond lengths (ABL) of Ti_nV clusters are shown in Figures 4a and 4b. The Ti-V bond length gradually increases from Ti_3V to $Ti_{15}V$ clusters, and exhibits two minima at Ti_6V and $Ti_{12}V$, and possibly $Ti_{16}V$, on the curve. Those sizes correspond to Ti_nV clusters that have stronger Ti-V bonds but less pronounced Ti-Ti bonds, indicating that these structures may have more delocalized V-Ti bonds. To prove that, we calculated the total density of

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4 states (DOS) of the Ti_nV clusters with the addition of the local density of states (LDOS) of
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6 the V impurity as shown in Figure 5. For simplicity, we present the DOS calculation without
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8 spin-polarization corresponding to the non-magnetic state. From the present DOS curve, we
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10 can observe that from Ti_1V to Ti_4V clusters, the total DOS have a molecule-like energy
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12 distribution with a number of localized peak features. That is to say, the V impurity affects
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14 the metallic behaviour of small Ti_n clusters. From Ti_5V onwards, and overlap between the
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16 energy levels leads to a continuous energy band which eventually continues to the bulk as
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18 the size increases. Ti_{12}V is a special case, in which a high peak is located at the Fermi level,
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20 giving us an insight of the high reactivity of the icosahedral cluster. Interestingly, the DOS
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22 curve for the Ti_{12}V coincide with that of the pure Ti_{13} cluster, which has been calculated
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24 with the *all-electron* method.⁵ For Ti_{12}V and its first neighbors, the V impurity LDOS is
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26 localized farther from the Fermi level, (at $E = -2$ eV from E_F), which explains the increase
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28 in stability for these clusters. However, except for the Ti_nV clusters studied in this work,
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30 the V impurity LDOS has a scarce contribution at the Fermi level. Since these clusters
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32 adopt the same structures than pure Ti_n , we expect that the reactivity properties are not
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34 significantly changed except for Ti_{1-2}V clusters, in which a larger highest-lowest occupied
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36 molecular orbital (HOMO-LUMO) gap may reduce the reactivity of the clusters.³⁵ This
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38 results motivate us for investigating Ti_nV_m bimetallic clusters which may offer opportunities
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40 for tuning the electronic properties with an appropriate composition.

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42 Recently, it was found that Ti-based nanomaterials have a high-capacity hydrogen stor-
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44 age.³⁶⁻³⁹ The chemical reactivity of small Ti_n clusters towards dissociative chemisorption of
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46 H_2 has been documented recently.⁵ These works suggest that the chemisorption of one H_2
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48 molecule has size dependent behaviour, with Ti_{13} being the most reactive cluster towards
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50 H_2 chemisorption. According to our present findings, we suggest that Ti_{12}M clusters which
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52 favor the encapsulation of the M-dopant atom (e.g., M=B, Al and presently V) are promis-
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54 ing, since titanium (the active site) remains on the surface. We are currently exploring the
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56 reactivity and electronic properties of the Ti_{12}M clusters when they are modified by differ-
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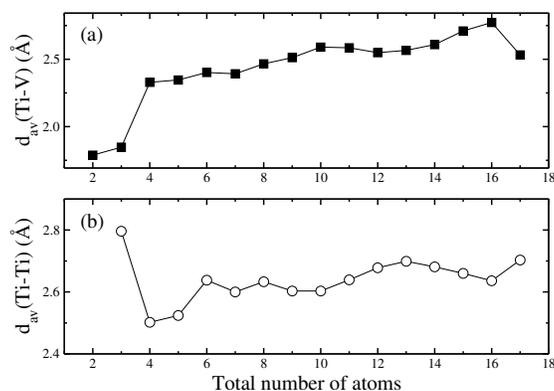


Figure 4: The Ti-V (a) and Ti-Ti (b) average binding distance of the most stable $Ti_n V$ clusters is presented.

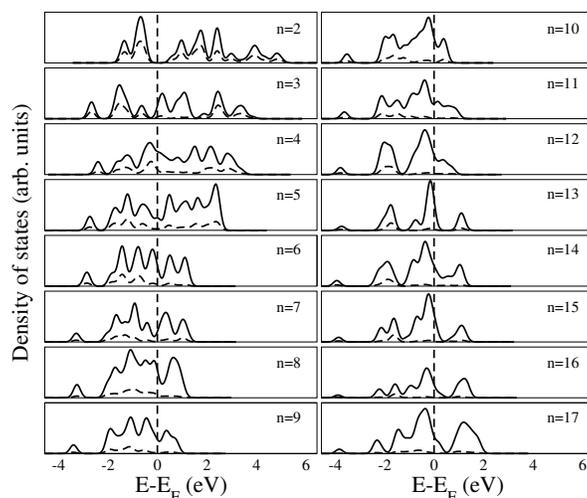


Figure 5: The total DOS of $Ti_{n-1} V$ clusters (solid curve) and LDOS of the V atom (dashed curve) is presented. A Gaussian broadening of 0.2 eV is used. The Fermi level is set at zero energy, denoted by a vertical dashed line.

ent impurity elements, with the belief to identify novel potential applications of M-doped Ti clusters.

Conclusions

In this work, the electronic and geometric structures of Ti_n and $Ti_n V$ ($n = 1 - 16$) have been investigated using density functional theory (DFT) calculations with the generalized gradient

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3 approximation (GGA). The lowest-energy structures of Ti_nV cluster have been determined
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5 by extensive searches for each cluster size. In the ground state structures of the Ti_nV clusters,
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7 the V atom prefers to occupy the surface site when $n \leq 8$ and $n = 16$, while for $n = 9$ up
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9 to 15, the V impurity falls in the center of the cage. Maximum peaks are observed for
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11 Ti_nV clusters at $n = 6, 12$ and 14 on the second-order energy difference, due to a relatively
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13 higher stability. We also found that when a single V impurity is added on Ti_n clusters an
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15 increase in the average binding energy occurs especially for $n = 12$, suggesting that the Ti_{12}V
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17 cluster favors the encapsulation of the V-dopant atom. We are also currently exploring the
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19 reactivity and electronic properties of the Ti_{12}M clusters when they are modified by different
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21 impurity elements, with the belief to identify novel potential applications of M-doped Ti
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23 clusters. Additionally, the electronic structures of small Ti_nV ($n \leq 4$) clusters exhibit a
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25 transition from metallic-like to semi-metallic electronic structure, while for $n = 5$ onwards,
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27 no significant changes are observed compared to pure Ti_n clusters. This results motivate
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29 us to investigate Ti_nV_m bimetallic clusters which may offer opportunities for tuning the
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31 electronic properties for appropriate and specific purposes.
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